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48, BD JOURDAN – E.N.S. – 75014 PARIS TÉL. : 33(0) 1 43 13 63 00 – FAX : 33 (0) 1 43 13 63 10 www.pse.ens.fr

Sons as Widowhood Insurance: Evidence from Senegal

Sylvie Lambert and Pauline Rossi*
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Abstract

Exploiting original data from a Senegalese household survey, we provide evidence that fertility choices are partly driven by women's needs for widowhood insurance. We use a duration model of birth intervals to show that women most at risk in case of widowhood intensify their fertility, shortening birth spacing, until they get a son. Insurance through sons might entail substantial health costs since short birth spacing raises maternal and infant mortality rates.

Keywords: Intra-household insurance, Gender, Fertility, Health, Senegal.

JEL Codes : D13, I15, J13, O15.

^{*}Sylvie Lambert: Paris School of Economics - INRA (sylvie.lambert@psemail.eu); Pauline Rossi: Paris School of Economics and CREST (pauline.rossi@ensae.fr). Dominique van de Walle sensitized us to the situation of widows in Sub-Saharan Africa, and qualitative field work in Senegal in her company proved very inspiring. The paper benefited from early discussions on son preference in Africa with Annamaria Milazzo. For their careful reading of our paper and their numerous suggestions we are grateful to Xavier d'Haultfoeuille, Luc Behaghel, Denis Cogneau, and Dominique van de Walle. The authors are also grateful for the comments of Guilhem Cassan, Nicolas Pistolesi, Maelys de la Rupelle, and participants to seminars at LMI - CREST, Namur University, Graduate Institute of International and Development Studies and CERDI and to conferences at Paris 1, ISS, NEUDC, Nanterre University and CSAE. We thank IDRC (International Development Research Center), INRA Paris and CEPREMAP for funding data collection, and the World Bank for funding qualitative field work. Work for this paper was supported by the World Bank's Knowledge for Change Program II under the research project "Welfare Impacts of Marital Status Shocks and the Implications for Social Protection Policy."

In many developing countries, the lack of insurance markets and social safety nets is mitigated by family. A large literature describes the use of family as insurance, mentioning for instance family income diversification strategy through migration (Rosenzweig, 1988), or children acting as old-age insurance for their parents (Nugent, 1985; Hoddinott, 1992).

In this paper, we analyze such a self-insurance mechanism – one whereby women in Senegal rely on sons as insurance in case of widowhood. As detailed below, we exploit the variation in widows' vulnerability that arises from the rivalry for inheritance between the husband's children. When the husband already has children from ex-wives, 1 whether divorced or deceased, the current wife's only way to secure future access to his resources – in particular his house – is to have a son. Hence, we investigate whether fertility choices are partly driven by women's insurance strategies. Our hypothesis is that the existence of children of ex-wives (henceforth we call these children "rivals") should exacerbate son preference and intensify fertility. Building on demographers' methodology, we use semi- and fully parametric estimations of a duration model of birth intervals to provide evidence that women with rivals and no son do indeed tend to have another child more quickly. We find that when there are rivals, having only girls versus having at least one son multiplies by 1.5 to 2 the probability of short birth spacing (intervals shorter than 24 months). In the absence of rivals, the gender composition of first births does not affect subsequent birth intervals. We show that the effect is clearly evidenced for women who co-reside with their husband, in particular for the poorest half of the population, justifying the prior that the house is the main stake in the bequest process. Also, fertility choices are more strongly affected after the third child.

In Senegal, women are highly exposed to the risk of losing their husbands, in particular because of the age difference between spouses: 10 years on average, and often much more. The question of the means available to women to cope with the impact of widowhood on living standards is a very urgent one. Formal mechanisms are weak: finance and insurance markets are very imperfect, social safety nets are missing, and opportunities for self-support are limited due to labor market restrictions and constraints stemming from social norms. Hence, widows are dependent on their access to their late husband's resources.

Furthermore, as 95 percent of the population is Muslim, inheritance practices are ruled by Islamic and customary patrilineal laws. In practice, wives are excluded from a bequest after

^{1.} Rivalry may also arise in polygamous unions between children of co-wives, but we choose not to consider them for two reasons. First, our identification strategy fails to deal with simultaneity issues: in polygamous unions, women might adjust the number of their children to react to a co-wife's births, so that the rivals of a given wife cannot be considered as exogenous to her own fertility choices. Second, it can be argued that co-wives have an alternative insurance strategy based on cooperation, since they may agree to continue to live together in the late husband's house (see qualitative evidence in Lambert and van de Walle, 2012).

the death of their husband; the inheritance is to be shared among the husband's children, sons inheriting more, and more frequently, than daughters (Lambert, Ravallion and van de Walle, 2013). Children, especially sons, therefore turn out to be women's best claim to their late husbands' resources in case of widowhood. Any children the husband had with other women may compete for the man's inheritance. Therefore, the number and gender composition of the children of the current wife, relative to other children the husband might have, determine the share of inheritance she might control de facto; it influences, in turn, her probability to carry on residing in the late husband's house. Women might therefore have incentives to be pregnant often in order to maximize the number of sons they have.

Demonstrating such a mechanism may matter if we are to better understand the costs of informal family insurance. Indeed, these costs are rarely studied; until recently, it was assumed that taking part in family insurance networks has no cost other than reciprocity. Recent papers have focused on the monetary costs for relatively high-income members, and on the distortions generated by the "kin tax" in African economies (Jakiela and Ozier, 2012). The monetary costs are often considered negligible for low-income members. Non-monetary costs have been totally overlooked, and yet they might be important from a welfare perspective. The cost of widowhood insurance through sons is potentially huge: health risks related to frequent pregnancies are well-documented in the medical literature on developing countries (e.g. Conde-Agudelo et al., 2006). Increasing the interval between births to 24 months is a goal for many family planning programs. ² On the child side, short birth intervals are associated with an increased risk of adverse perinatal outcomes: lower birth weight, smaller infants for gestational age, higher risk of preterm delivery, stillbirth and neonatal death. In Senegal, children born less than two years after a sibling are 2.4 times more likely to die than the others, whatever mortality rates we consider: neonatal, post-neonatal, infant, juvenile, infant-juvenile (ANSD and ICF International, 2012). 3 On the mother's side, studies in Latin America (Conde-Agudelo and Belizan, 2000) and in Bangladesh (DaVanzo et al., 2004) demonstrate that women with birth intervals lower than 15 months bear a significantly higher risk of maternal complications. One medical explanation is the maternal depletion hypothesis, stating simply that short intervals do not allow the mother to recover from

^{2.} Some programs such as the Optimal Birth Spacing Initiative, created under the auspices of USAID, even recommend an optimal birth spacing of three to five years.

^{3.} Ronsmans (1996) shows that in rural Senegal, short birth intervals also increase the odds of dying for the preceding child: if the mother delivers another child within two years, the risk of mortality for the index child is four times higher in the second year of life than if the next birth takes place more than two years after his birth. However, this correlation is not necessarily causal: short subsequent birth intervals may be either a cause (abrupt weaning) or a consequence (willingness to "replace" a dead child) of child mortality.

the physiological stresses imposed by the previous pregnancy. In the economics literature, Milazzo (2012 and 2013) finds that son preference induces short birth spacing, and might be a significant cause of female excess adult mortality in Nigeria and India.

Further, in Senegal, maternal and infant mortality rates are a matter of concern: out of each 1,000 births, four mothers died as well as 47 children before turning a year old – 29 of those in the first month, over the period 2007-2011 (ANSD and ICF International, 2012). Reducing maternal and child mortality as well as implementing birth control are two key objectives of the Senegalese national health development plan (called PNDS-II, covering 2009-2018). On the supply side, the budget of the Health Ministry was multiplied by 3.5 between 2000 and 2010, reaching 108.4 billion FCFA (about 220 millions dollars), and now accounts for 10.4 percent of the national budget (ANSD and ICF International, 2012). A great deal of effort has been made to increase access to maternal health care services, in particular tetanus toxoid injections to pregnant mothers and child-delivery assistance by skilled professionals. However, efficient supply-side interventions require understanding people's behaviors: why do frequent pregnancies persist at such a large scale? Women's needs for widowhood insurance might be part of the answer.

Exploiting original data from a nationally representative household survey, we develop a strategy that is close to a difference-in-difference framework. We analyze how the gender composition of the first children influences subsequent choices of women with and without rivals. While the two groups might have other differences, what matters to our identification strategy is that (i) the gender of the children they give birth to is exogenous, and (ii) in the absence of rivals, both groups would have reacted similarly to this exogenous variable: having one son vs. one daughter. Using such a strategy to identify the existence of a widowhood insurance motive for fertility is very similar in spirit to Nugent's (1985) suggestion: in order to evidence old-age security motive, one has to compare similar populations with different intensity of the motive. Here, among women with rivals, we compare those having a son and those having only daughters; they are similar, but the strength of their motivation is different. Then, we factor in women without rivals to cancel out any son preference that prevails in the population but is not related to widowhood insurance.

All in all, we find that son preference only appears in women with rivals, and especially when these women have no independent housing. Women's needs for widowhood insurance seem therefore to play a role in fertility choices, leading to more frequent pregnancies for the most exposed women: those with rivals and no son. This suggests that the lack of formal widowhood insurance hampers birth control efforts and, even more worryingly, imposes a

potentially heavy health cost on both women and children, whether widowhood occurs or not. Such non-monetary costs underline the fact that, even if an informal insurance system plays a role in granting access to resources in case of widowhood, it is a poor substitute for a formal insurance scheme. The benefits of implementing some public widowhood insurance scheme, or changing inheritance laws, would thus be far reaching.

The outline of the paper is as follows. Section 1 provides background on widowhood and inheritance practices in Senegal. Section 2 presents the data and some descriptive statistics. Section 3 discusses the empirical strategy, the identification assumptions and the methods of estimation. Section 4 reports the main results, and Section 5 concludes with policy implications.

1 Widowhood and Bequest in Senegal

1.1 An ex-ante risk-coping strategy based on children

An idea has emerged from several disciplines, that women's vulnerability in Sub-Saharan Africa is conducive to large family size. ⁴ Family law renders women dependent on spouses, or on adult children in case of death or abandonment by the husband. Women therefore have an interest in early marriage and high fertility. Anthropologists such as Bledsoe (1990) also endorse the idea that in all societies, people make efforts to construe marital status and parenthood to their advantages. She claims that in Africa, as long as children remain women's best claim to male resources, women will continue to want many children.

Demographers working on Sub-Saharan Africa have come to the same conclusion: among the key factors shaping the reproductive regime in this region, they mention inheritance patterns and women's subordinate status. In patrilineal societies, in which wives "belong" to the male kin, women's security and status critically depend on their ability to have sons (Lesthaeghe, 1989).

All this requires that fertility is an active choice of women. In Senegal, modern contraceptive methods are widely known, but not much used: over 92 percent of married women can name at least one modern method (sterilization, oral contraceptive, implants, IUD, condom); but only 12 percent – mostly urban, educated and wealthy women – report using one of them. Still, only 7.5 percent of married women report unmet needs for birth control to limit the number of children. This proportion is even smaller for younger women: around 4.5 percent

^{4.} In Senegal, fertility is still high: five is both the average and median number of children among women older than 45 years (cf. Figure 2 in Appendix A).

for women between 15 and 39 years old. Unmet needs for birth control to increase intervals between births are higher, though (22 percent). Another way to assess whether women do indeed have some control over their fertility is to look at the percentage of unwanted or unplanned pregnancies. Only 4 percent of pregnancies that occurred during the period 2005-2010 are reported by the mothers as unwanted and 20 percent as unplanned (ANSD and ICF International, 2012).

A majority of Senegalese women therefore claim to be choosing the number of children they have and, to a lesser extent, choosing the timing of births. One explanation is that birth spacing is partly determined by breastfeeding amenorrhea and abstinence, and the period of breastfeeding is in the domain of the mother. So women may have some control over the spacing of births, even in the absence of modern contraceptive methods, as argued by some anthropologists Mace and Sear (1997). In Senegal, the median postpartum non-susceptible period (related to amenorrhea and/or abstinence) is 14 months, and the average 15 months (ANSD and ICF International, 2012).

1.2 The bequest process

In Senegal, women have little access to inheritance as daughters, and even less as wives. Indeed, as described in Lambert et al. (2013), the Islamic inheritance law is the dominant rule in the country, despite the existence of an alternative possibility; in particular, wills and testaments are rarely made, and even less often implemented. De jure, the Islamic rule entitles wives to one eighth of the total bequest, to be shared among all wives in case of polygamous union. In practice, women are generally excluded from the bequest. Further, this inheritance system splits the bequest between the children, ⁵ limiting the inheritance of daughters to half of that of sons. In addition, entrenched tradition favors sons for inheriting land. ⁶ Since daughters typically move to their husband's abode, they are supposedly compensated by their brothers, with money or other forms of wealth, for what would have otherwise been their share of land inheritance; the same holds with respect to inheriting the father's house. But in practice, the compensation does not always take place. In our data, among people who lost their father, we find that daughters are significantly less likely to report that the father left a bequest, and among those who do, daughters are 2.5 times more likely to have not received anything (10 percent vs. 4 percent); they are also less likely to inherit land or a

^{5.} A man's extended family (uncles, cousins, nephews, etc.) is entitled to a share of the bequest only if he died childless.

^{6.} A small exception is the Basse Casamance region, where there is slightly more access to land for women, due to strong tradition in women-dominated rice cultivation.

house, but not significantly more likely to inherit money, which contradicts the compensation story.

Another reason why daughters might be deprived of their rights is the non-implementation of the inheritance process. Typically, brothers and their own families may stay together in the father's house after his death; as long as they are willing to live together, they do not feel the need of an actual division of property to take place and may consider that the father left no bequest. Among people who reported no bequest, we find that sons are significantly more likely to live in the household of their late father. If we consider that in such a case the house is transmitted de facto, we can estimate the proportion of people who inherited (part of) a house: 60 percent of sons vs. 49 percent of daughters. This might not seem such a large imbalance. Nevertheless, when one looks at women at the time of their own death rather than at the time of their parents' death, it appears that women are vastly less likely than men to bequeath a house: less than a quarter of adults whose mother died have inherited anything from her, and only 22 percent of those who did inherited a house. By contrast, 72 percent of adults whose father died have inherited something, and 71 percent of them inherited a house. This significant gap between men and women in the possibility to transfer property rights at the time of their own death suggests that, even if a large fraction of women claim to have inherited a house and hence appear to feel entitled to part of the house property, this might be only a temporary situation. In fact, by the time they die, they seem to have lost any access to it.

In total, men seem to be more successful than women at claiming their inheritance rights and in holding on to their property. As a result, the share of the bequest that will accrue to a woman's children will depend not only on the number but also on the gender composition of her offspring, relative to rivals. Having at least one son is a necessary condition to insure some access to the bequest when the husband had children from a previous union.

Further, having a son might not only raise the likelihood of remaining in the house, but could also provide an alternative in case of eviction. Indeed, widows are more likely to be hosted by a son than a daughter: among widows hosted by their children, 92 percent live with one son vs. 34 percent with one daughter. If we further consider widows living with exactly one child, 68 percent live with one son vs. 32 percent with one daughter, and both situations are very different: widows are hosted by their sons in two thirds of the cases, while they host their daughters in two thirds of the cases (being head of household, or remarried and co-residing with the new husband).

1.3 The vulnerability of widows

So far, the economic literature on vulnerability has paid little attention to the situation of widows in Sub-Saharan Africa. Yet, a few papers highlight that women are extremely vulnerable to the loss of their husbands: households headed by widows are significantly poorer than male-headed and other female-headed households (Appleton, 1996 in Uganda; Horrell and Krishnan, 2007 in Zimbabwe). In Mali, van de Walle (2011) finds that widowhood has a strong, lasting impact on women's living standards and welfare indicators: the detrimental effects persist over time even if women remarry, and the disadvantage is passed on to children. The vulnerability of widows stems from women's subordinate status regarding legal protection, individual endowments, social norms and access to and control over resources. Historians have also documented that women who lack male support, like widows, are more vulnerable in case of famine (see Vaughan, 1987 for the history of a famine in Southern Malawi in 1949).

Vulnerability is exacerbated when women have rivals for their husbands' resources. The question of wives' rivalry has only been studied in the context of polygamous households. Researchers working on Mali have documented that co-wife rivalry is responsible for resource-consuming struggles (Kazianga and Klonner, 2006); it even adversely affects child survival, especially that of sons since they remain to compete for land (Strassmann, 1997).

In this paper we are interested in the competition with children of ex-wives, rather than with co-wives. The existence of children of at least one ex-wife is a common feature in the Senegalese context where widowhood, divorce and remarriage are very frequent for both men and women. Antoine and Dial (2003) point to the lack of reliable data on divorce in Africa: cross-sectional studies often underestimate the frequency of divorce because remarriage happens quickly. Using a biographical approach, they find that one union in three ends with a divorce in Dakar; 25 percent of divorces occur after less than seven years of marriage, and 50 percent of divorced women are remarried five years later. To our knowledge, there are no studies about the impact of past marriage of the husband on current wife's well-being.

For current wives, the main stake in case of widowhood is probably the husband's house. First, notably for poor households, the house is likely to be the main asset. Second, according to qualitative evidence, women fear being thrown out of the house by the children of an exwife and having nowhere to go (Lambert and van de Walle, 2012). For instance, a childless widow reported how she was confronted by the children of her husband after his death: they offered her a room to rent in their father's house at a steep price that she could not pay, and she was forced to leave. Clearly, this fear is relevant only for women that were not housed

independently from their husband. Finally, remaining in the house of the late husband can be a way either to avoid the obligation of remarrying, or in case of remarriage, to keep a relatively high degree of autonomy in this new marriage.

These two dimensions are illustrated in Table 1 in which we provide some statistics on widows, broken down by the place of residence after the husband's death. Widows in our data were on average 46 years old when they lost their husband, 7 and children were born from this union in the vast majority of cases (88 percent). Two out of three widows were able to remain in the same household after the death of their husband, while the other third joined another household. Among those who could remain in the same household, 90 percent still reside there at the time of the survey: they became head of household, or stepped aside for one of their children. Only 20 percent got remarried, and among those who did, only one third live with their new husband. The story is completely different for widows hosted by another household at the death of their husband. 8 They generally joined up with their parents, a child or a sibling. The host family provided only temporary accommodation: in 75 percent of the cases, widows had moved to another place at the time of the survey, after a stay shorter than two years for half of them. Consistently, the fraction of remarried women living with the new husband is much higher in this population: 48 percent remarry, and among those, two thirds live with their new husband. Hence, women who remained in their late husband's house were more likely to have avoided remarriage, and if they remarried to be non-coresiding. For married women, non-coresidence seems to be a favorable situation. In Senegal, nearly a quarter of married women do not co-reside permanently with their husband. It is in particular the case for women who have their own house, which may be inherited from a previous husband now deceased. In cases where spouses do not co-reside, the husband has another dwelling and comes for regular visits. Women who do not co-reside seem to benefit from greater autonomy and enjoy relatively higher per-capita consumption levels (De Vreyer and Lambert, 2013). Therefore, even if other possibilities exist, remaining in the late husband's house is associated with a gain in autonomy for the rest of the life, even in the event of a remarriage.

It is important to note that the argument that women need a son to guarantee access to the husband resources is likely to be less relevant for women without rivals, even if the probability of termination of this union is clearly positive. In Senegal, there is no legal

^{7.} According to World Development Indicators, life expectancy at birth for women in Senegal is 62 years old.

^{8.} Here, the decision to leave the husband's house may be either taken by the widow herself, or imposed on her.

provision for alimony and maintenance allowance for children. Hence, the divorcee does not obtain anything from the ex-husband, whatever the number of children. In addition, at the death of the ex-husband, not only is the ex-wife not entitled to any share of the inheritance, but even if her children obtain the house, she would not return to live in the abode of a man she divorced, or who repudiated her. First, she is likely to be remarried and would keep the living arrangements she has with her current husband, and second, in such a patrilineal society, it would not be conceivable that she return as household head in the house of a former marriage that belongs to another lineage. Hence, a first wife who has no rivals has no incentive to adjust her fertility to mitigate the impact of the termination of that union.

2 Data

2.1 The survey "Poverty and Family Structure"

The data used here come from an original survey entitled "Poverty and Family Structure" (PSF) conducted in Senegal in 2006-2007 (detailed description in DeVreyer et al., 2008). ⁹ It is a nationally representative survey conducted on 1,800 households spread over 150 primary sampling units drawn randomly among the census districts. About 1,750 records can be exploited.

In addition to the usual information on individual characteristics, the survey obtained a comprehensive description of the household structure. Of particular relevance for our purposes is the fact that the survey registers for each child how many half-siblings he has, counting separately siblings from the same father only, siblings from the same mother only and siblings from both the same parents. Therefore, we are able to identify the children from previous unions on the mother's side, and the rivals on the father's side: since we consider monogamous unions only, all siblings having the same father but a different mother than the current wife, are children of an ex-wife. There is also information on all children below age 25 of household members, even if they do not live with their parents. Children who died are also reported but there is no information on the timing of births. As a result, a woman's complete birth history for surviving children is available only if all her children are under 25 years old. Among the children registered, only 59 percent live with both their parents; the

^{9.} Momar Sylla and Matar Gueye of the Agence Nationale de la Statistique et de la Démographie of Senegal (ANSD), and Philippe De Vreyer (University of Paris-Dauphine and IRD-DIAL), Sylvie Lambert (Paris School of Economics-INRA) and Abla Safir (now with the World Bank) designed the survey. The data collection was conducted by the ANSD.

figure is similar to the national average (ANSD and ICF International, 2012). When parents do not live together, children live with their mothers in two thirds of the cases. That is why standard household surveys would largely underestimate the number of rivals, or even ignore their existence.

Moreover, detailed information is collected on all current spouses, whether they co-reside or not, and on past marital history of all members (age at first marriage, being or not in the first union). This can be relevant since having previous unions, or children from previous unions, might play a role in determining women's current fertility. Lastly, we use information on education, occupation and income, as additional controls.

2.2 Descriptive statistics on women

The sample consists of 936 women under 39 years old, engaged in monogamous unions, with at least one child from the current union. We had to restrict the sample of interest to relatively young women to ensure that their complete birth history is known, as mentioned above. In our data, the lower bound for age at first birth is 13, so children of women below 39 years old are all younger than 25. Since birth cohort is orthogonal to other variables of interest, this selection will not induce any estimation bias. Further, we focus on a given woman's children with her current husband, because they are the ones at stake during the bequest process.

Table 2 gives an overview of important characteristics of these women. For some of them, observations are missing for one or more variables. We have all the information for only 761 women, on whom we perform the semi- and fully parametric estimations. ¹⁰ The table provides the descriptive statistics for both the full sample and the subsample with complete information. They do not differ in any notable way. Non-parametric estimations are carried out on the full sample of 936, and we comment below on the descriptive statistics on this sample. Women have on average 2.7 living children with their current husband; the number ranges from 1 to 9 (Figure 2 in Appendix A displays the distribution). Roughly one woman in five has lost at least one child, and 4 percent have children from previous unions. Of course, since they are in the middle of their reproductive lives, we do not observe their total fertility. The average age in the sample is 28, while the median ages at births 2 and 3 are respectively 25 and 28 years old. ¹¹ We will therefore focus on children of rank 1, 2 and 3; only a small

^{10.} Table 11 in Appendix A provides the detail of the number of observations with missing values.

^{11.} The median age at birth 2 and 3 is derived from the sample of women above 45 years old, who have reached the end of their reproductive life.

fraction in our sample has already given birth to more children. Fertility varies significantly across places of residence, education levels and employment status; in our sample, 48 percent of women live in rural areas, 44 percent received no education at all, and 33 percent work. Regarding their marital lives, the vast majority of these women (87 percent) are in their first union; the remainder have only one broken union. Women marry for the first time at age 19 on average, and they marry a much older husband: the age difference is 10 years on average, and up to 23 years in the top decile of the distribution of age differences. The threat of becoming a young widow is therefore probably a widespread matter of concern. Only 7 percent of husbands work in the public sector, so the public system of widowhood pensions covers a very small part of the population. The average annual income is 1.6 million FCFA (approx. 2,500 euros), but it is driven by the right tail of the distribution as 50 percent of the husbands earn less than 500 K FCFA annually (approx. 750 euros). Turning to statistics about rivals, marrying a man who already has children with ex-wives is not unusual: 17 percent of women have at least one rival, and 12 percent at least one male rival. The number of rivals in inheritance shares (1 share = 1 boy = 2 girls) is on average 1.7, but the variance is large with numbers ranging from 0.5 to 7.5 shares. 10 percent have strictly more rivals than own children at the time of the survey.

Women marrying a divorced man or a widower are described in Panel A of Table 3. They have themselves more complex marital lives: they are older and more likely to have broken unions, in which children were born. The age difference with their husband is significantly higher, by four years. They are also more likely to live with their current husband, and to work. A first hint that the presence of rivals may have an impact on fertility is that women with rivals have on average more children with their current husband, and in quicker succession. As predicted by the medical literature, shorter birth intervals are correlated to a higher mortality rate for those children.

A subsample of particular interest will be that of co-residing wives. ¹² As explained in the preceding section, rivalry for inheritance seems to be mostly about the husband's house; hence, the threat of being thrown out of the house by rivals only jeopardizes women who

^{12.} One caveat is that co-residence status is observed at the time of the survey, and not when fertility choices were made. Consequently, some women are considered as co-residing, though they were housed independently when their children were born. If they anticipated that they would eventually join their husband's house, they should indeed be included in the category of most exposed women. Conversely, some women are considered as non-coresiding, while they used to live with their husband. In our sample, out of 231 non-coresiding women, 46 actually remained with their family-in-law after the husband, generally for professional reasons, left the household. Those women clearly face the same risk of eviction as co-residing ones. We find that, indeed, they behave similarly: when we include them in the subsample of co-residing wives, the magnitude and significance level of our coefficients remain completely unchanged.

actually live in their husband's house. It is therefore natural to look at the potentially most exposed women to find evidence of insurance strategies. As shown in Panel B of Table 3, only three married women in four live with their husband. Non-coresiding wives are very similar to other women in terms of socioeconomic characteristics (age, area of residence, education, occupation), but they tend to have fewer children, both dead or alive, with their current husband.

Note that we cannot exhibit any descriptive statistics on widows with rivals and no son, since, consistently with our claim, there are very few of them (11) in the sample. If we believe that the widowhood insurance mechanism is at play, such a situation would indeed be rare.

3 Empirical Strategy

3.1 A duration model of birth intervals

The basic idea underlying our empirical strategy is to compare fertility choices and son preference of wives with and without rivals. We build on the literature on son preference to devise an empirical strategy based on duration models of birth intervals (Leung, 1988, 1991). The existence of son preference is confirmed when the length of the birth interval before the next child is longer for couples with more sons.

The advantage of duration models is their ability to deal properly with right-censored observations, i.e. families that are not yet complete by the time of the survey. ¹³ Indeed, they allow us to identify the distribution of a duration variable from potentially right-censored observations as long as the duration and the right-censoring variables are independent. This condition is very likely to be satisfied here, as the date of the survey is completely unrelated to the latest births. Another rationale for considering birth intervals is to account for health risks related to the spacing, and not only to the number, of births.

Using duration models, son preference has been tested and validated by an extensive literature focusing mainly on Asia: in China (Tu, 1991), Bangladesh (Rahman and Da Vanzo, 1993), the Chinese population of Malaysia (Pong, 1994), Vietnam (Haughton and Haughton, 1995), India (Arnold et al, 1998), South Korea (Larsen et al., 1998), and Taiwan (Tsay and Cyrus Chu, 2005).

^{13.} We have only limited information on the children of women with complete fertility: among women over 45 years old who declare having at least one child, not a single child is found in our dataset in almost half of the cases; all the children are found in only 7 percent of the cases. On average, a woman declares five children and only 1.3 is registered.

Only a few papers examine this question in an African context: ¹⁴ Gangadharan and Maitra (2003) find evidence of son preference in South Africa, but only among the Indian community. To our knowledge, the only conclusive paper on African data using duration models was written by anthropologists working on Gabbra pastoralists in the North of Kenya; they find that women with no son have significantly shorter subsequent birth intervals than women with at least one son (Mace and Sear, 1997). They relate son preference to the patrilineal and patrilocal family system prevailing among the Gabbra. Hence, evidence on son preference is quite limited in Sub-Saharan Africa.

3.2 The model with proportional hazard

To test whether son preference is related to the presence of rivals, we use a model with proportional hazard. Our variable of interest T is the duration between successive births, measured in months. Our coefficients of interest measure the impact of the gender composition of the first children on the subsequent birth interval, among wives with and without rivals. We consider intervals between births n and (n+1) for $n = \{1, 2, 3\}$. We start by running a pooled regression of all intervals, and then separate regressions for each of the three parities to determine the one at which hazard rates diverge.

The key element of duration models is the hazard function: the instantaneous probability to have another child at date t. In the specification with proportional hazard, the hazard function is modeled as follows:

$$\lambda(t) = \lambda_0(t) \times \exp(X_n'\beta)$$

Where $\lambda_0(t)$ is the baseline hazard function, common to all individuals, and X_n is a vector of individual covariates at birth n susceptible to influence the hazard function. Then the survival function – the probability not to have another child at least until t – is as follows:

$$S(t) = \Pr(T > t) = \exp(-\int_0^t \lambda_0(u) du \times \exp(X_n'\beta))$$

^{14.} Some papers use duration models of birth intervals in Africa, but they are interested in the impact of socioeconomic factors (e.g. mother's characteristics like birth cohort, age at first marriage and at first birth, residence, and education in Ghilagaber and Gyimah, 2004), not in son preference. Other papers deal with son preference in Africa, but do not estimate duration models; for instance, Milazzo (2012) estimates a linear model for the probability of short birth interval to convincingly underline the role of son preference in the fertility choices of Nigerian women.

^{15.} As a robustness check, we will include all parities instead of limiting up to parity 3. See section 4.3.

In our case, X_n includes:

- Girls: a dummy equal to 1 if the first n children are all girls.
- Rivals: a dummy equal to 1 if there is at least one rival. As robustness checks, we consider alternative definitions of rivals, such as the number of rivals or a dummy equal to 1 for at least one male rival.
- Girls \times Rivals: the interaction term between Girls and Rivals.
- Additional characteristics of the woman related to fertility: age at birth n, area of residence, level of education, age at first marriage, whether in her first marriage, living or not with her husband, having at least one dead child, ¹⁶ having at least one child from previous unions.
- In the pooled regression, we also include n: the rank of preceding birth, to control for potential differences between parities.

The fact that we do not observe the birthdate of deceased children might lead us to overestimate the true duration between all successive births, and hence to underestimate son preference. If women do indeed shorten birth spacing until they get a son, we would wrongly assign a large birth interval to those who lost a child as a consequence. Our coefficients can therefore be viewed as a lower bound for son preference.

Also, one might worry about selective mortality: those women who intensify their fertility when they have only daughters are more at risk of maternal death, and therefore more likely to be under-represented in the sample. But this would again lead us to underestimate son preference. Moreover, we find no evidence of selective mortality among women with female firstborns: in our data, girls are not more often maternal orphans than boys. ¹⁷

3.3 Identification assumptions

Under the proportional hazard assumption, each covariate X_k has a multiplicative effect that is constant over time on the hazard rate. e^{β_k} might therefore be interpreted as the hazard ratio at any point in time between two individuals that only differ by one unit of X_k . The proportional hazard assumption will be tested when estimating the model.

In our case, β_1 , β_2 and β_3 are the coefficients on Girls, Rivals and $Girls \times Rivals$, respectively. e^{β_1} measures the hazard ratio between women having only daughters and women having at least one son, among those without rivals. β_1 identifies a causal impact if the gender

^{16.} This is the best we can do to mitigate the fact that we do not observe all successive births; results are qualitatively unchanged if the dummy is removed.

^{17.} Among children younger than 15 years old (6,150 observations), 2.4 percent of boys and 2.5 percent of girls have lost their mothers. The difference between boys and girls is not significant (p-value=0.82).

composition of the first children is truly exogenous. This assumption is likely to hold insofar as there is no evidence of sex-selective abortion or infant mortality in Senegal (ANSD and ICF International, 2012). In our sample, sex ratios among children are perfectly balanced (cf. Figure 3 in Appendix A). Moreover, we test that women having n daughters are indeed similar to women having at least one son for $n = \{1, 2, 3\}$: balancing tests presented in Appendix A, Table 12, provide some level of reinsurance that the Girls dummy is exogenous. ¹⁸ If we find that $e^{\beta_1} > 1$ (in other words, having only daughters vs. at least one son increases the hazard rate and hence decreases the expected birth interval) then we can infer the existence of son preference among women without rivals.

 $e^{\beta_1+\beta_3}$ measures the same ratio among women with rivals. Therefore, e^{β_3} is the odd-ratio that captures the difference in son preference between women with and without rivals. If our hypothesis is true, then we expect $e^{\beta_3} > 1$; in other words, having only daughters vs. at least one son should increase *more* the hazard rate and decrease *more* the expected birth interval when there are rivals. β_3 would identify an insurance strategy through sons as long as both groups of women have the same "intrinsic" son preference, meaning outside of inheritance considerations.

Of course, wives with and without rivals are different; even after controlling for observable differences, some unobservable characteristics may drive both fertility choices and the decision to marry a divorced man or a widower. ¹⁹ However, what matters for our identification to hold, is that in the absence of rivals, both groups would have reacted similarly to an exogenous shock: having one son vs. one daughter. Under this assumption, if wives with rivals eventually display a stronger son preference than wives without rivals, the difference would be caused by the presence of rivals. In Section 4, we run some placebo tests to ensure that (i) the common "intrinsic" son preference is plausible, and that (ii) an insurance-based interpretation explains the results better than potential alternative mechanisms.

One limitation of our empirical strategy is that we are dealing with rather small samples. Table 11 in Appendix A gives details about the number of observations for each estimation, as well as the exact number of observations in each cell of interest. In particular we should keep in mind when interpreting the results that there are very few women having three daughters, no son and some rivals.

^{18.} We conduct univariate t-tests to compare covariates' means across both subsamples, and we find no statistically significant difference at 5 percent when $n = \{1, 2\}$ and only one (in 17 covariates) when n = 3.

^{19.} It is worth underlining that, given the general complex patterns of marital lives in Senegal, marrying a divorced man or a widower is likely to happen to most women at some point in their lives.

3.4 Descriptive statistics on birth intervals

Table 4 presents some descriptive statistics of our duration variables. When we pool all durations together, durations after birth 1 account for almost half of the observations, durations after birth 2 for one third, and the remaining durations are observed after birth 3. A bit more than one third of the durations are right-censored, a proportion that logically increases in parity. Among non-censored observations, the distribution is quite similar for the 3 parities, with a mean around 36 months, and a median around 30 months. One fourth of the births would be considered as risky with a birth spacing lower than 24 months. Note that duration between births 1 and 2 displays a larger variance due to "extreme" values. ²⁰

Before estimating the proportional hazard model, the first step to get a picture of the survival function is to compute the Kaplan-Meier estimator of S(t) (Kaplan and Meier, 1958). The two left hand side graphs of Figure 1 show it plotted when durations are pooled together and when they are separated by parity. Both graphs display a common shape with three important features:

- 1. $\widehat{S}_{KM}(t) = 1$ if t < 8: the shortest birth interval is equal to 8 months.
- 2. The exit rate is increasing until approximately 50 months and then decreasing.
- 3. $\widehat{S}_{KM}(t) > 0$ even if t is large i.e. the distribution of T is defective; in other words, some women will never have an additional child.

Also, note that we observe "jumps" in the survival function at 12, 24, 36 etc. months. They are due to measurement approximations: in roughly one third of the non-censored cases, we do not observe the exact dates of birth for the children n and (n + 1), hence we approximate the birth interval by the age difference multiplied by 12, to get the duration in months. The same approximation is implemented on censored observations in 20 percent of the cases, when the exact birthdate of the latest child is missing.

As a consequence, when we observe t_n , the information we derive is more or less precise, depending on the type of observation:

- Not censored, precisely measured; we infer that $T_n \in [t_n 1; t_n + 1]$.
- Not censored, imprecisely measured; we infer that $T_n \in [t_n 12; t_n + 12]$.
- Censored, precisely measured; we infer that $T_n > t_n 1$.

^{20.} Approximately 2 percent of birth intervals are larger than eight years (mostly observed after birth 1). In half of the cases, women have in fact lost one or two children in the meantime; the remaining cases are mostly urban, educated, working women living in relatively rich households.

^{21.} See Appendix B for further details about the approximation and the number of observations of each type.

- Censored, imprecisely measured; we infer that $T_n > t_n$.

This will be dealt with when we estimate a fully parametric version of the model.

Using the Kaplan-Meier estimate of the survival function and its variance, it is possible to test for the equality of distributions between two sub-populations (log-rank tests). 22 The log-rank tests are conclusive in two cases: first, when n=3, we reject the null (at 11 percent) that women with 3 daughters and rivals have the same survival function than the rest of the population. Second, in the pooled specification, when we restrict the sample to co-residing wives, we also reject the null (at 3 percent) that women with only daughters and rivals have the same survival function as the others. As shown by the right hand side graphs of Figure 1, the survival function of women having only daughters and rivals is systematically below that of the others, which means shorter birth intervals.

The non-parametric estimation provides a first hint that women with the highest need for widowhood insurance also make different fertility choices.

3.5 Estimation methods

3.5.1 Semi-parametric estimation

We start by considering a semi-parametric estimation of the Cox proportional hazard model (Cox, 1972). Using a partial likelihood, the method of estimation makes it possible to estimate the vector of coefficients β without imposing a functional form on $\lambda_0(t)$. The idea is to focus on the ordering of events rather than on the exact duration for each observation. ²³ In the pooled specification, we use robust standard errors clustered at the woman level to account for the correlation between the error terms related to the different birth intervals for the same woman.

One can derive an estimate of the baseline survival function, $\widehat{S}_0(t^*_{(j)})$, constant by pieces on the interval $[t^*_{(j)}; t^*_{(j+1)}]$, where $t^*_{(1)} < ... < t^*_{(k)}$ are the k ordered distinct values among non-censored observations (Box-Steffensmeier and Jones, 2004). We use it to compute the

^{22.} We compare women with only daughters vs. those with at least one son; women with rivals vs. those without any; and finally women with both only daughters and rivals vs. others.

^{23.} In the three separate regressions, we use the exact marginal-likelihood method to handle ties among non-censored durations. It provides the most accurate and appropriate approximation when duration data is generated by a continuous time process and ties arise from imprecise measurement, as is the case here, because it takes into account all the possible orderings of tied failures. We check that estimates based on alternative approximations (Efron or Breslow method) are of very similar size and significance. In the pooled regression, we use Breslow as the exact marginal-likelihood method is not available when standard errors are clustered.

expected duration conditional on X for the women who eventually have another child: 24

$$\mathbb{E}(T \mid X, T \leq t_{(k)}^*) = \left(\sum_{j=1}^{k-1} \widehat{S}_0(t_{(j)}^*)^{\exp(X'\hat{\beta})} \times (t_{(j+1)}^* - t_{(j)}^*)\right) - t_{(k)}^* \widehat{S}_0(t_{(k)}^*)^{\exp(X'\hat{\beta})}$$

Another quantity of interest is $(1 - \widehat{S}(24 \mid X))$: the probability of a short birth interval for women with characteristics X. We define "short" as less than or equal to 24 months because it is the minimum length advocated by family planning programs and used in health statistics (e.g. the Demographic and Health Surveys (DHS) Program) below which a birth is considered risky.

Nonetheless, the semi-parametric estimation has three main limitations. First, it is not well-designed to model individual-level unobserved heterogeneity, which would be useful here to capture the unobserved determinants of fertility across women (e.g. fecundity level). Second, the specific measurement approximations described above cannot be accounted for with the standard Cox estimation. Third, the estimation does not explicitly take into consideration the defective distribution of our durations.

3.5.2 Fully parametric estimation

To account for (i) unobserved heterogeneity, (ii) measurement approximations, and (iii) a defective distribution, we estimate a fully parametric multispell model. The details of the specification are given in Appendix C.

Unobserved heterogeneity (ν) is introduced in the hazard function. The baseline hazard is defined so as to reproduce two characteristics of the durations observed in our sample : (i) there is no exit before eight months, and (ii) the inverted U shape of the exit rate arises from the combination of an increasing baseline hazard together with unobserved heterogeneity. ²⁵

Further, the contribution to the likelihood of each observation is specified in a way that takes into account measurement approximations; it uses a confidence interval that depends on how precisely the duration is measured, instead of the density and survival function.

Finally, we model explicitly the probability to stop having children after the n^{th} birth. We are thus able to disentangle the effect of covariates, in particular Girls, Rivals and

^{24.} In the Cox model, some women will never have another child, so the global expected duration would be equal to infinity. That is why our quantity of interest is in fact the expected duration given that $T \leq t_{(k)}^*$.

^{25.} Women with a high hazard rate exit at the beginning, and after some time only women with a low hazard rate remain. We do not investigate further whether the inverted U shape results from the exit process per se, or from the variation in the composition of the population, because in this study we are not mainly interested in duration dependence.

 $Girls \times Rivals$, on the number of births and on the spacing of births.

We start by constraining the parameters to be the same for all parities and compare the estimates to those found in the pooled Cox regression. Then we allow the parameters 26 to vary depending on n, and compare the estimates to those found in the three separate Cox regressions. In the last specification, in order to keep enough degrees of freedom, we constrain the model and keep only the controls whose impact was significant in the estimation on all parities.

Last, we are able to compare the probability of having another child, the expected birth interval and the probability of short birth spacing, across different categories of women.

4 Results

4.1 Semi-parametric estimation: Results

We first discuss the estimates of the pooled specification (Table 5), and then turn to the results disaggregated by parity (Table 6). When we consider the whole sample of monogamous women under 39 years old having at least one child from the current union, there is no ratio significantly different from 1; we notice that in magnitude, e^{β_1} and e^{β_2} are indeed very close to 1, whereas e^{β_3} is higher, but imprecisely estimated.

In accordance with the hypothesis that the crux of the matter lies with the access to the house, we consider the subsample of co-residing wives. For them, we have information about the husband's characteristics (income, sector of activity, age difference) that we include in the regression as additional controls; we also add a dummy indicating whether the woman works. e^{β_1} remains insignificant, so we find no detectable evidence of son preference among women without rivals, at least up to their third child. e^{β_3} is higher in this subsample, and now significantly different from 1 (at the 5 percent level). Hence, among women co-residing with their husband and with at least one rival, the hazard rate is multiplied by $e^{\beta_1+\beta_3}=1.6$ for those having only daughters as compared to those having at least one son.

We further investigate whether the presence of rivals has a heterogeneous impact depending on the socioeconomic status of the household; to do so, we split the sample of co-residing wives on the median income. ²⁷ In the poorest half of this population, e^{β_3} is very high and

^{26.} Except the standard deviation of the unobserved heterogeneity. This is precisely the strength of the multispell model: random draws from the normal distribution are attributed once and for all to each individual, explaining simultaneously all durations.

^{27.} Results are qualitatively unchanged if we take education instead of income as an indicator of socioe-conomic status: e^{β_3} is much higher for non-educated women than for educated ones. The same is true if we

significant (at 1 percent): having only daughters multiplies the hazard rate by 2.4 for women with rivals, while it has no significant impact for women without rivals. In the richest half of the population, e^{β_3} is not significantly different from 1. ²⁸ At first sight, such a result might seem at odds with standard economic predictions that the larger the bequest, the stronger the incentives to take hold of it. However, what matters in our context is probably not the absolute value of the bequest as much as the relative value of the house in the bequest; and the house is the main asset in most of poor households. Moreover, women in those households have hardly any alternative in case of eviction because they cannot rely on personal resources or on their extended family to support them.

Another group of women particularly exposed to the risk of widowhood would be those married to an old husband. However, we would need more women married to an old enough husband to be able to estimate the effect of husband's age. 29

Also, note that e^{β_2} is never different from 1. Hence, after controlling for observable differences between women with and without rivals, both groups make similar fertility choices once they have a son.

Next, we consider the three regressions corresponding to each parity for the whole sample; the only ratio significantly different from 1 is e^{β_3} when n=3. Among women with at least one rival, the hazard rate is multiplied by 2.5 for those having three daughters as compared to those having at least one son.

The results disaggregated by parity suggest that the presence of rivals impacts fertility choices particularly after the third child, and for the women who have not had a son yet. The average ideal family size among married Senegalese women is five children (ANSD and ICF International, 2012). Hence, the vast majority of women probably expect to have other "tries" for a son, when at first they have one or two daughters. The pressure to have a son would start increasing after the third "missed try," once some women have reached their ideal family size. We predict that the effect should keep growing at parities 4 and 5, but

split the sample according to the rural/urban divide. In this case, we find that e^{β_3} is very large for rural women, while none of the coefficients is significantly different from 1 in the urban subsample.

^{28.} If we interact a *Poor* dummy with our variables of interest instead of splitting the sample, the difference between rich and poor is confirmed: the coefficient on the triple interaction $Girls \times Rivals \times Poor$ is equal to 2 and significant at 10 percent.

^{29.} The distributions of husband's age at birth n are : $Q_1 = 27, Q_2 = 31, Q_3 = 36$, among women without rivals; and $Q_1 = 30, Q_2 = 36, Q_3 = 42$, among women with rivals. They are vastly overlapping. The impact of husband's age on women's choices is likely to be non-linear, but the relevant thresholds are difficult to figure out. Indeed, the mortality risk is increasing with age, but maybe not in a way that is very perceptible by wives: 0.41 percent for men aged 35 to 39, 0.55 percent for those aged 40 to 44 and 0.58 percent for those aged 45 to 49 (ANSD and ICF International, 2012).

unfortunately, our sample size does not allow us to test this prediction. ³⁰

Regarding the controls, hazard ratios are in line with expectations. The hazard rate decreases with parity: durations are longer between the latest children. It is higher for women in their first union and who married younger. Also, it is higher for co-residing wives, in particular when n=3: the hazard rate doubles. The area of residence has a significant impact, especially when $n=\{2,3\}$: the hazard rate is multiplied by approximately 1.5 for rural vs. urban mothers. Two covariates play a significant role only when n=1: the hazard rate is halved for mothers who already have children from previous unions; and the hazard rate is 25 percent lower for women having one dead child, suggesting that our dummy variable mainly captures the death of children after the first child and before the second (living) child.

When we restrict the sample to co-residing wives, we find that women married to civil servants, and therefore entitled to a public system of widowhood pensions, have lower hazard rates (30 percent lower); the effect is particularly strong for the richest half of the population. Age difference and employment status of the woman never have a significant effect.

We test the proportional hazard assumption following the procedure developed by Grambsch and Therneau (1994) and based on the Schoenfeld partial residuals (Schoenfeld, 1982). We fail to reject it in the pooled specifications, and when $n = \{2, 3\}$, which supports the choice of our model. But we reject the proportional hazard assumption when n = 1, both in the global test and in the tests for education and dead children variables. To further investigate whether the violation of this assumption introduces a strong bias in our coefficients of interest, we split the sample according to the median duration between births 1 and 2 and run separate regressions on both subsamples. We find that, indeed the effect of the education and dead children variables are not constant in time, 31 but β_1 , β_2 and β_3 are not different for shorter and longer durations.

To better understand the consequences of these results in terms of health, we estimate (i) the expected birth spacing and (ii) the probability of short birth spacing for the three populations in which we detected an effect: co-residing wives, the poorest half of co-residing

^{30.} Jayachandran and Kuziemko (2011) have also put forward the hypothesis that gender is most predictive of subsequent fertility near ideal family size in India. They build a formal model of fertility choices under son preference, in which breastfeeding acts as a contraceptive. They predict that the probability of breastfeeding should be lowest for daughters without older brothers; and the gender gap is expected to rise once ideal family size is reached.

^{31.} The lack of education has a positive impact on hazard rates (hence a negative impact on durations) only for shorter durations. And having one dead child has a negative impact on hazard rates (hence a positive impact on durations) only for larger durations: this seems consistent as the death of a child has a mechanical positive impact on the duration between births 1 and 2 only if it occurred between them – and this cannot be the case if the duration is short.

wives, and women with at least three children (cf. Table 7). We consider the median individual as the reference individual, by setting the values of the controls to the median of the sample. ³²

Among co-residing wives, we find that, holding everything else constant, the expected birth spacing is quite similar for all women when there is no rival. But in presence of rivals, having only daughters vs. at least one son is predicted to reduce birth spacing by 10 months and to multiply the probability of short birth spacing by 1.5. These same figures are 11 and 2, respectively, when we consider the poorest half of the population. ³³

If we turn to the sample of women with at least three children, having three daughters vs. at least one son reduces the expected birth spacing by 13 months and doubles the probability of short birth spacing among women with rivals. In contrast, it has almost no impact among women without rivals, and if any, it is the other way around.

The probability of very short birth spacing (below 15 months) ³⁴ is multiplied by 1.5 for co-residing wives and by 2.3 for women in relatively poor households, and for those having three daughters.

4.2 Fully parametric estimation: Results

The estimates of the fully parametric specification are reported in Tables 8 and 9; they confirm, strengthen and specify the results of the Cox model.

The first clarification is that, on the one hand, our variables of interest Girls, Rivals and $Girls \times Rivals$ have no significant impact on the probability to stop having children, whatever sample we consider. ³⁵ But on the other hand, the effect of $Girls \times Rivals$ on durations is much higher and significant than estimated in the Cox model; e^{β_3} turns out to be significant even for the whole sample. The ranking across subsamples remains the same: e^{β_3} is still larger for co-residing wives, in particular for the poorest half, and for women with at least three children. Otherwise, e^{β_1} and e^{β_2} are similar in magnitude to the Cox estimates, and in the same way, never significantly different from 1.

Hence, estimations based on the explicit modeling of a defective distribution suggest that women's needs for a son influence the spacing, but not the number of births – at least up to

^{32.} We check that results are qualitatively unchanged if we consider the average individual (not shown).

^{33.} Excluding extreme values of birth intervals (above 96 months) does not change the predicted probability of short birth spacing, but mechanically reduces the expected birth spacing and flattens out differences between categories: the gap between women having rivals and only daughters vs. at least one son amounts to 6 and 8 months, for co-residing wives and for the poorest half of co-residing wives, respectively.

^{34.} Same computation as for the probability of birth spacing below 24 months (not shown).

^{35.} The probability of having another child is estimated to be around 98 percent for the median individual, irrespective of the gender composition of the first children and/or the presence of rivals.

the third child. Our results are in line with the literature on son preference: Jensen (2005) and Basu and De Jong (2010) point out that son preference does not necessarily lead to differences in sibship size when fertility is high; in this case, they advocate looking at birth intervals to find evidence of son-preferring behavior.

Further clarification is also obtained on the controls. Living in a rural area, being married for the first time, and co-residing with the husband, all make it significantly less likely to stop having children; coefficients are particularly high when n=3, as already noted in the Cox estimation.

Other controls influence birth spacing: the age at first marriage, the rank of the child and having children from previous unions increase durations; whereas the age at the previous birth and a low level of education tend to shorten durations. Again, we find that having one dead child has a significant, positive impact on durations only between births 1 and 2. Co-residence is the sole variable influencing both the number of children and their spacing.

When we introduce controls related to the husband, marrying a civil servant has a mixed impact on fertility: it reduces the probability to stop, but it also lengthens durations. Age difference and women's employment remain insignificant.

Our quantities of interest capturing the magnitude of the effect display larger differences across groups than those derived from the Cox estimation: ³⁶ in the presence of rivals, having only daughters vs. at least one son multiplies the probability of short birth spacing by 2 to 4 times; the reduction in the expected birth spacing is estimated between 11 and 21 months, depending on the population we consider. But just as in the Cox model, birth spacing is predicted to be quite similar for all women when there is no rival (cf. Table 10).

Regarding the baseline survival function, coefficients are always precisely estimated. The graphs corresponding to different populations of interest and to different parities, are plotted in Appendix D, Figure 4. When we consider all parities together, the baseline survival function of co-residing wives is always below the one of the whole sample, reflecting their increased fertility.

Last, in all specifications, estimates of the variance of the unobserved heterogeneity are significant at the 1 percent level and of the same order of magnitude. ³⁷

^{36.} Here again, we compute these quantities for the median individual (setting $\nu = 0$).

^{37.} We find $\sigma = 0.68$ for the whole sample, 0.75 for co-residing wives, and 0.63 when coefficients are parity-specific.

4.3 Robustness and placebo tests

We further perform robustness and placebo tests reported in Appendix E. First, we check that hazard ratios in our main subsample of interest – co-residing wives – are robust to alternative specifications: (i) including all parities instead of limiting up to parity 3; and (ii) adding controls for ethnic groups (Table 14). If anything, when all parities are included, e^{β_1} increases slightly and borders significance (p-value=0.16), suggesting that son preference may appear at higher parities even in the absence of rivals. Nevertheless, son preference remains significantly stronger for women with rivals. Coefficients are also unchanged when we control for previous durations in the regressions by parity (not shown).

Second, one can wonder whether the results of the pooled regression are actually only driven by durations after birth 3. It would be somewhat worrying due to the small number of women having three daughters and rivals. To remove any doubt, we focus on durations after birth 1 and consider the sample of co-residing wives, as a whole and next divided into poorest half and richest half. ³⁸ As shown in Table 15, results of the pooled regression still hold when we consider only durations after birth 1 : e^{β_3} remains of the same order of magnitude and significance level. So the mechanism seems to be already at play after birth 1 but to a lesser extent, so that the impact of insurance strategies on fertility would be only detectable for the most exposed women. After birth 3, the pressure would be much stronger and the effect visible in the whole population.

Third, we check that our estimates do not capture preferences for diversity rather than son preference, by replacing the *Girls* dummy by a *Boys* one: we find that having only sons vs. at least one daughter has no significant impact on the hazard rate, either for women with or without rivals; if anything, the ratio is always lower than one, which refutes the hypothesis of preferences for diversity (Table 16).

Fourth, we test the identification assumption of a common "intrinsic" son preference between women with and without rivals. The reasoning is the following: if one son is already enough to feel insured, women with rivals should display the same son preference as women without rivals from the moment they give birth to their first son. Restricting the sample to women of parity 2 with at least one son, we find indeed that the impact of having two sons vs. one son and one daughter is the same in the two groups; women with two sons wait significantly longer before getting pregnant again, irrespective of the presence of rivals

^{38.} We did the same exercise on durations after birth 2 : estimates are line with the pooled results, even though not significant, but we should be careful with the interpretation due to the small sample size when n=2.

(Table 17).

Fifth, we investigate an alternative explanation for higher son preference in the presence of rivals, which emphasizes the role of the husband. One story is that husbands would be more likely to divorce, or repudiate, a first wife if she had not given birth to a son; the next wife would then feel the pressure to have a son quickly to avoid divorce or repudiation. Such a mechanism is very improbable in our case since there are slightly more boys than girls among rivals, and also slightly more ex-wives with at least one son than ex-wives with at least one daughter.

Another story assumes that men with a strong son preference would be more likely to take another wife in order to maximize the number of sons they have, and the arrival of a new wife could prompt the first one into divorcing; $e^{\beta_3} > 1$ would simply capture the son preference of the husband, not of the wife. If this were true, we should observe evidence of son preference among the rivals, since the husband would have put pressure on his first wife as well. We have no systematic, detailed information on the timing of births of the rivals so we cannot use a duration model of birth intervals. Instead, we test a standard prediction of son-preferring, differential stopping fertility models: under son preference, an average girl is predicted to have more siblings than an average boy (Jensen, 2005, Basu and De Jong, 2010). It is not the case for the rivals in our sample: boys and girls have on average 2.5 siblings. Hence, husband's son preference does not seem to drive the results.

Last, we consider alternative definitions of rivals to capture potential effects of the gender composition and the number of rivals. ³⁹ So far, our results indicate that the presence of one son plays a crucial part in the inheritance process. If we turn the reasoning around, rivals should represent a threat (i) only when there are male rivals and (ii) as soon as there is one male rival.

We begin with defining rivals as a dummy equal to 1 if there is at least one male rival, thus excluding women having only female rivals from the category. As shown in Tables 18 and 19, the same pattern of results observed in the specification "at least 1 rival" holds. Also if we compare the effect of having at least one male rival vs. one female rival in our sample of interest – co-residing wives – e^{β_3} is smaller and no longer significant in the female case. When we introduce both, the coefficient on $Girls \times Rivals_male$ is 35 percent higher than the coefficient on $Girls \times Rivals_female$, even though both are not significant (Table 20). So indeed, the threat to inheritance is constituted by male rivals.

We then test whether the effect is linear in the number of rivals. In order to do so, we

^{39.} Note incidentally that the coefficients on the controls are robust to alternative definitions of rivals.

create a variable equal to the number of rivals in inheritance shares (Tables 21 and 22). Again, e^{β_3} is particularly high for the poor and after the third child. Among co-residing wives, each additional inheritance share for the rivals increases the hazard ratio between women having only daughters and women having at least one son by 23 percent. However, the impact of the number of rivals is non-linear: most of the effect takes place between 0 and 1 rival; each additional rival raises the ratio only slightly. Among women with exactly one rival, having only daughters doubles the hazard rate. Logically, the effect is entirely driven by women having one male rival; it is zero for women having one female rival (Table 23).

One minor difference in the estimates using alternative definitions is that e^{β_2} is sometimes significantly lower than 1 for the poorest half of co-residing co-wives and for women with at least three children. But the ratio is imprecisely estimated, and in any case, of relatively small magnitude. It only suggests that women with more and/or male rivals tend to have larger birth intervals than other women as long as they have at least one son: one son seems enough to feel insured.

5 Conclusion

All in all, we find that wives with rivals for inheritance need to have one son, while there is no detectable sign of son preference for wives without rivals, at least up to their third child. These findings support the idea that sons play a key role in insuring women in case of widowhood. However, the impact of insurance strategies on fertility only materializes for the most exposed women: those with no independent housing, with rivals and without a son among the first children. The cost of insurance through sons in terms of health is therefore borne by a small fraction of women: in cross-section, they represent only 7 percent of our sample. ⁴⁰ But, from a longitudinal perspective, the fraction of women concerned at some point in their life should be much higher given the high rates of divorce and remarriage in Senegal.

Still, for these women and their children, the health risk is huge. We showed that the probability of short birth spacing was multiplied by 1.5 to 2, and up to 4 for some subpopulations; and we know from the medical literature that short birth spacing multiplies the risk of infant death by 2.4 (ANSD and ICF International, 2012) and doubles the risk of maternal death (Conde-Agudelo and Belizan, 2000).

^{40. 75} percent of women currently live with their husband and among them, 18 percent have rivals and 50 percent have a female firstborn.

As a consequence, reducing women's reliance on children to eventually disassociate fertility choices from insurance considerations could help achieve the national health plan's objectives. The general consensus is that improving women's status is a precondition for the fertility transition. In a chapter entitled "Women's agency and social change," Amartya Sen argues that women's empowerment will bring about lower fertility rates and lower infant mortality (Sen, 1999). However, Sen maintains that the main drivers of fertility transition are (i) a change in women's aspirations and bargaining power, and (ii) access to birth control methods. We argue that both conditions are necessary, but not sufficient: as long as women have no alternative insurance strategies, they will continue to have many children to mitigate downside risks, starting with widowhood.

One might think of three, non-mutually exclusive, ways ahead. First, reforming inheritance rules to grant wives, irrespective of the number of children, a significant percentage of the husband's wealth, or at least the usufruct of the house for some years. Second, expanding social benefits to protect a larger share of the population: in the Senegalese case, it would be broadening to all widows the current system of pensions paid to the widows of civil servants. Third – but in the longer run, given the difficulties encountered by insurance companies in developing countries – promoting formal insurance and financial markets.

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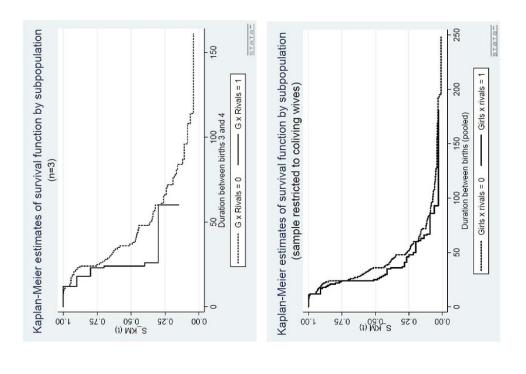
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FIGURE 1: Non-parametric estimation of survival functions (pooled and separated by parity and by sub-population)



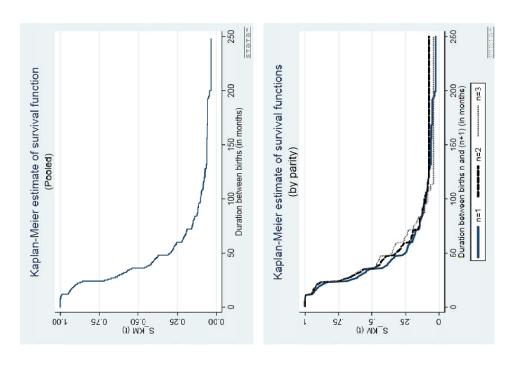


Table 1: Widows' characteristics, by place of residence after the husband's death

		Remained in the	Hosted by
		same household	another household
Observations		364	182
Average age at husband's death		49.5	38.5
Still in the household	(at the date of the survey)	90%	25%
If not : median length of stay	(in years)	7	2
	The widow herself	45%	20%
	A child	30%	13%
Household head	A parent	4%	23%
	A sibling	6%	12%
	Other	15%	32%
Remarried		20%	48%
If remarried, co-residing	(with the new husband)	35%	67%

Sample: women whose latest broken union ended with the husband's death (statistics computed for the latest period of widowhood); only 20 percent of them have experienced more than one broken union.

TABLE 2: Descriptive statistics: Sample of women under 39 years old, engaged in a monogamous union, having at least one child from current union

	All women	Women with no
		missing observations
Number of observations	936	761
Number of children from current union	2.7 (1.63)	2.7 (1.64)
At least one child from previous unions	4.1%	3.9%
At least one dead child (from current union)	19.8%	19.8%
Age	27.9 (6.02)	28.0(6.05)
Rural	48.4%	47.6%
No education	43.8%	43.9%
Work	32.8%	32.8%
First union	86.6%	88.3%
If not: nb broken unions	1.1 (0.38)	1.1 (0.35)
Age at first marriage	18.9 (4.30)	19.0 (4.35)
Live with their husband	75.3%	77.9%
If co-residing: Age difference	10.2 (6.54)	10.2 (6.33)
If co-residing: Public sector	7.3%	7.8%
If co-residing: Annual income K FCFA (median)	500	500
At least 1 rival	17.1%	16.8%
At least 1 male rival	11.9%	11.3%
Average nb of rivals (inheritance shares)	1.7 (min 0.5; max 7.5; s.d. 1.38)	1.6 (min 0.5; max 7.5; s.d. 1.38)
Strictly more rivals than children (inheritance shares)	9.7%	9.1%

Standard deviations are in parentheses. The second column presents statistics on women for whom there is no missing observation; we perform the semi- and fully parametric estimations on this subsample.

Table 3: Descriptive statistics: Comparisons

	A. Wives with and without rivals At least one rival No rival p-val	nd without No rival	rivals p-value	B. Co-residing	B. Co-residing and non co-residing wives Co-residing Non co-residing p-value	ing wives p-value
Number of observations	159	770		705	231	
Number of children from current union	3.1	2.6	0.01***	2.8	2.1	0.01***
At least one child from previous unions	10.7%	2.6%	0.01***	3.4%	%0.9	0.12
At least one dead child (from current union)	26.7%	18.5%	0.04**	21.2%	15.2%	0.04**
Interval between births 1 and 2 (in months)	33.3	36.8	0.10*	35.3	40.6	0.05**
Age	30.2	27.5	0.01***	27.9	28.0	0.93
Rural	44.7%	49.5%	0.27	48.9%	46.8%	0.56
No education	40.6%	44.6%	0.37	44.0%	43.0%	0.79
Work	40.5%	30.8%	0.02**	32.8%	32.9%	0.98
First union	78.5%	88.8%	0.01***	92.9%	66.5%	0.01***
If not: nb broken unions	1.2	1.05	0.14	1.0	1.1	0.08*
Age at first marriage	19.2	18.8	0.29	18.7	19.4	0.04**
Live with their husband	81.2%	74.8%	*20.0			
If co-residing : Age difference	13.7	9.5	0.01***			
If co-residing: Public sector	8.7%	7.0%	0.52			
If co-residing : Annual income K FCFA (median)	200	200	0.83			
At least 1 rival				18.3%	13.4%	*20.0
At least 1 male rival				12.9%	8.9%	0.08*
Average nb rivals (inheritance shares)				1.7	1.7	0.81

We conduct t-tests comparing the means of each covariate, and a nonparametric equality-of-medians test for the income : a low p-value indicates that both subsamples are statistically different with respect to the corresponding covariate.

The total number of observations in panel A is different from 936 because there are 7 missing values for the presence of rivals.

^{***} Significant at the 1 percent level. **Significant at the 5 percent level. * Significant at the 10 percent level.

Table 4: Statistics on non-censored durations

	Pooled	Parity #1	Parity #2	Parity #3
Total number obs	1939	904	644	391
Number non-censored obs	1250	634	395	221
Number of months				
Mean	36.2	36.4	35.9	36.2
Std dev.	21.3	23.3	18.5	19.8
Min	8	8	8	8
Q1	24	24	24	24
$\mathrm{Q}2$	30	30	31	30
Q3	45	44	47	48
Max	200	200	120	114
Number obs ≥ 96 months	29	20	5	4

Statistics computed on non-censored durations, expressed in months.

Approx. 2% of birth intervals are larger than 8 years: in half of the cases, women have in fact lost 1 or 2 children in the meantime. The remaining cases are mostly urban, educated, working women living in relatively rich households. Results are qualitatively unchanged if we exclude extreme values (above 96 months) from the sample.

Table 5: Cox estimation (pooled)

Hazard ratios = e^{β_k}	Whole sample	Co-residing wives	Poorest half	Richest half
	(1)	(2)	(3)	(4)
Girls	1.00	1.07	1.08	1.04
	(.069)	(.088)	(.118)	(.137)
Rivals	1.03	0.94	0.78	1.01
	(.108)	(.112)	(.133)	(.164)
Girls imes Rivals	1.23	1.54**	2.26***	1.21
	(.217)	(.334)	(.612)	(.395)
Baseline controls	Yes	Yes	Yes	Yes
Additional controls	No	Yes	Yes	Yes
Log-likelihood	-6569	-4607	-2111	-1956
Observations	1589	1117	569	548
Clusters	761	515	260	255
Obs in cell : $Girls \times Rivals = 1$	93	64	36	28

Robust standard errors of e^{β_k} are in parentheses (clustered at the woman level) - Significance levels (for $e^{\beta} \neq 1$):*** Significant at the 1 percent level. *Significant at the 5 percent level. *Significant at the 10 percent level.

Girls : first children are only girls ; Rivals : there is at least one rival.

Column (2): sample restricted to wives living with their husband; this sample is then split on the median income into the poorest half in column (3) and the richest half in column (4).

Baseline controls mainly include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, rank of preceding birth. Additional controls include: occupation of the wife, sector of activity of the husband, income of the husband, age difference with the husband.

Table 6: Cox estimation (separated by parity, whole sample)

Hazard ratios = e^{β_k}	Parity #1	Parity #2	Parity #3
\overline{G}	0.98		
	(.095)		
Rivals	0.92		
	(.158)		
$G \times Rivals$	1.35		
	(.323)		
GG		1.07	
		(.149)	
Rivals		1.30	
		(.211)	
$GG \times Rivals$		0.90	
		(.300)	
GGG			0.79
			(.204)
Rivals			0.82
			(.161)
GGG imes Rivals			3.20**
			(1.548)
Controls	Yes	Yes	Yes
Log-likelihood	-1889	-1199	-645
Observations	737	528	324
Obs in cell: $Girls \times Rivals = 1$	57	26	10

Standard errors of e^{β_k} are in parentheses. Significance levels (for $e^{\beta} \neq 1$): *** Significant at the 1 percent level. *Significant at the 1 percent level.

 $G,\,GG,\,GGG:$ first n children are girls; Rivals: there is at least one rival.

Controls include characteristics of the mother : age at birth n, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions.

Exact marginal-likelihood method to handle ties among non-censored durations.

Table 7: Quantities of interest derived from Cox estimation

Co-residing wives	Girls = 0	Girls = 1	Girls = 0	Girls = 1
	Rivals = 0	Rivals = 0	Rivals = 1	Rivals = 1
Expected birth spacing in months	38.2	36.7	39.5	29.8
Probability of birth spacing ≤ 24 months	33.0%	35.9%	32.4%	47.6%
Poorest half (of co-residing wives)	Girls = 0	Girls = 1	Girls = 0	Girls = 1
	Rivals = 0	Rivals = 0	Rivals = 1	Rivals = 1
Expected birth spacing in months	36.0	35.1	38.5	27.5
Probability of birth spacing ≤ 24 months	33.8%	36.0%	27.5%	54.3%
n=3 (within whole sample)	GGG = 0	GGG = 1	GGG = 0	GGG = 1
	Rivals = 0	Rivals = 0	Rivals = 1	Rivals = 1
Expected birth spacing in months	35.8	39.0	38.5	25.4
Probability of birth spacing ≤ 24 months	35.1%	28.9%	29.8%	59.2%

 $\overline{\text{Expected birth spacing}} = \overline{\mathbb{E}(T \mid X, T \leq t^*_{(k)})}$

Probability of birth spacing $\leq 24 \text{ months} = 1 - \widehat{S}(24 \mid X)$

We use the baseline survival functions estimated in the Cox model (pooled specification for the first two panels, and n=3 specification for the last one).

We set the values of the controls to the median of the sample. We check that results are very similar if we set the values of the controls to the sample mean (not shown).

Table 8: Fully parametric estimation (same parameters for all parities)

Hazard ratios = e^{β_k}	Whole sample	Co-residing wives	Poorest half	Richest half
	(1)	(2)	(3)	(4)
Girls	1.01	1.03	1.19	0.97
	(.106)	(.124)	(.195)	(.160)
Rivals	0.97	1.02	0.69	1.08
	(.147)	(.179)	(.172)	(.288)
$Girls \times Rivals$	1.60**	2.29***	3.87***	1.79
	(.387)	(.653)	(1.440)	(.863)
Baseline controls	Yes	Yes	Yes	Yes
Additional controls	No	Yes	Yes	Yes
Log-likelihood	-2950	-2134	-908	-1203
Observations	761	515	260	255

Standard errors of e^{β_k} are in parentheses. Significance levels (for $e^{\beta} \neq 1$): *** Significant at the 1 percent level. *Significant at the 1 percent level.

Girls : first children are only girls ; Rivals : there is at least one rival.

Column (2): sample restricted to wives living with their husband; this sample is then split on the median income into the poorest half in column (3) and the richest half in column (4).

Baseline controls mainly include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, rank of preceding birth.

Additional controls include: occupation of the wife, sector of activity of the husband, income of the husband, age difference with the husband.

Table 9: Fully parametric estimation (parameters specific to each parity, whole sample)

Hazard ratios= e^{β_k}	Parity #1	Parity #2	Parity #3
\overline{G}	1.02		
	(.130)		
Rivals	1.00		
	(.217)		
$G \times Rivals$	1.47		
	(.447)		
GG		1.03	
		(.179)	
Rivals		1.38	
		(.286)	
$GG \times Rivals$		0.82	
		(.344)	
GGG			0.86
			(.263)
Rivals			0.85
			(.207)
$GGG \times Rivals$			7.46***
			(4.767)
Controls †		Yes	
Log-likelihood		-2935	
Observations		761	

Standard errors of e^{β_k} are in parentheses. Significance levels (for $e^{\beta} \neq 1$): *** Significant at the 1 percent level. *Significant at the 1 percent level.

 \dagger In this specification, the model is constrained to ensure a manageable number of parameters. In the logit, we keep only the variables whose impact was significant in the estimation on all parities: place of residence, being or not in her first marriage, living or not with the husband. In the survival function, we keep our variables of interest and the controls with a significant impact: age at birth n, level of education, age at first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions.

G, GG, GGG: first n children are girls; Rivals: there is at least one rival.

Table 10: Quantities of interest derived from fully parametric estimation

Co-residing wives	Girls = 0	Girls = 1	Girls = 0	Girls = 1
	Rivals = 0	Rivals = 0	Rivals = 1	Rivals = 1
Expected birth spacing in months	38.1	37.6	37.8	27.1
Probability of birth spacing ≤ 24 months	20.5%	21.1%	20.8%	42.7%
Poorest half (of co-residing wives)	Girls = 0	Girls = 1	Girls = 0	Girls = 1
	Rivals = 0	Rivals = 0	Rivals = 1	Rivals = 1
Expected birth spacing in months	35.5	33.3	40.8	23.6
Probability of birth spacing ≤ 24 months	22.8%	26.4%	16.4%	56.1%
n=3 (within whole sample)	GGG = 0	GGG = 1	GGG = 0	GGG = 1
	Rivals = 0	Rivals = 0	Rivals = 1	Rivals = 1

n=3 (within whole sample)	GGG = 0	GGG = 1	GGG = 0	GGG = 1
	Rivals = 0	Rivals = 0	Rivals = 1	Rivals = 1
Expected birth spacing in months	37.6	40.2	40.4	19.5
Probability of birth spacing ≤ 24 months	23.5%	20.6%	20.4%	77.0%
·				

Expected birth spacing = $\mathbb{E}(T \mid X, \nu = 0, \hat{\theta})$

Probability of birth spacing ≤ 24 months $= 1 - S(24 \mid X, \nu = 0, \hat{\theta})$

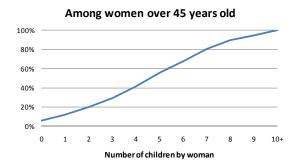
We use the survival function and the parameters estimated in the fully parametric specification (same parameters for all parities in the first two tables, and parameters specific to n=3 in the last table).

We set the values of the controls to the median of the sample. We check that results are very similar if we set the values of the controls to the sample mean (not shown).

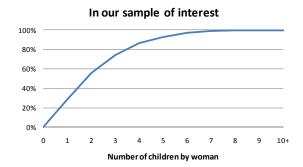
Appendix: For online publication

Appendix A: Additional descriptive statistics

FIGURE 2: Cumulative distribution of the number of children by woman



Sample: Women over 45 years old in the PSF survey (1060 observations) Distribution in line with national statistics reported in DHS-MICS, 2010-11.



Sample: Women below 39 years old, engaged in a monogamous union, having at least one child from current union (936 observations).

FIGURE 3: Sex ratio by age, among children from current union

Percentage of girls, by age interval 60% 55% 45% 40% 0-3 3-6 6-9 9-12 12-24*

Sample: All children from current union of the 936 women in our baseline sample. Percentages are unchanged if we include the 72 children from previous unions.

^{*} The last age interval is larger to reach a sufficient number of observations (see below).

Age interval	0-3 years	3-6 years	6-9 years	9-12 years	12-24 years	Total
Observations	739	632	441	276	363	2451

Table 11: Number of observations: Breakdown by missing variables and cells of interest

		Pooled	Parity #1	Parity #2	Parity #3
Initial number obs		2016	936	666	414
Twins		27	9	7	11
Missing duration		50	23	15	12
Number observations	(non-parametric estimation)	1939	$\boldsymbol{904}$	644	391
At least 1 missing obs		350	167	116	67
	sex children	2	2	0	0
	rivals	14	7	4	3
	previous children	0	0	0	0
	age	0	0	0	0
Missing:	rural	0	0	0	0
	education	64	27	21	16
	age first marriage	93	51	27	15
	first union	124	55	45	24
	co-residing	0	0	0	0
	dead children	111	50	41	20
Number observations	(parametric estimation)	1589	737	528	$\bf 324$
	Girls = 1	505	365	140	43
	Rivals = 1	270	112	91	67
Among which:	$Girls \times Rivals = 1$	93	57	26	10

The "pooled" column brings together all birth intervals, which are then split by parity; the 1589 observations correspond to 761 different women. But the duration between children 1 and 2 is missing for a few of them, that is why we have only 737 observations when n = 1.

Sample: Women below 39 years old, engaged in a monogamous union, having at least one child from current union.

Girls: first n children are only girls, Rivals: there is at least 1 rival.

TABLE 12: Balancing tests: Having only daughters vs. having at least one son

		Parity #1			Parity #2			Parity #3	
	G=0	G=1	p-value	GG=0	GG=1	p-value	GGG=0	GGG=1	p-value
Nb observations	372	365		388	140		281	43	
Nb children (in current union)	2.6	2.7	0.39	3.3	3.5	0.17	4.1	4.4	0.13
Children from previous unions ≥ 1	4.0%	3.8%	0.89	2.6%	2%	0.23	2.8%	2.3%	0.84
Dead children (in current union) ≥ 1	18.8%	20.8%	0.50	25%	18.6%	0.11	26%	34.9%	0.25
Age	27.9	28.1	0.59	29.3	29.6	09.0	31.1	30.8	0.71
Rural	49.7%	44.3%	0.15	50.3%	50.7%	0.93	52.7%	58.1%	0.50
No education	45.7%	42.7%	0.42	45.6%	43.6%	0.68	46.3%	55.8%	0.25
First union	90.1%	86.6%	0.14	91.5%	85.7%	0.08*	92.2%	97.7%	0.05**
If not : nb broken unions	1.1	1.05	0.62	1.1	1.05	0.87	1.1	1.0	0.08*
Age at first marriage	19.0	19.0	0.89	18.7	18.3	0.28	18.4	18.2	0.76
At least 1 rival	15.3%	16.7%	0.61	17.5%	18.6%	0.78	21%	25.5%	0.52
At least 1 male rival	9.1%	12.0%	0.20	11.1%	15%	0.25	12.8%	18.6%	0.36
Average nb rivals (in inheritance shares)	1.4	1.8	0.13	1.5	2.1	*60.0	1.6	2.0	0.41
Currently working	32.8%	32.6%	0.96	32.9%	32.1%	0.86	33.3%	27.9%	0.47
Co-reside with the husband	76.3%	79.4%	0.31	82.0%	85.0%	0.40	83.6%	88.4%	0,38
If co-residing: Age difference	10.0	10.4	0.36	10.1	10.8	0.28	10.2	12.2	0.07*
If co-residing: Husband in public sector	%9.9	9.5%	0.21	6.9%	8.6%	0.57	4.8%	8.1%	0.49
If co-residing: Annual income K FCFA (median)	480	009	0.07*	200	009	0.50	200	310	0.43

We conduct t-tests comparing the means of 16 covariates, and a nonparametric equality-of-medians test for the income: a low p-value indicates that both subsamples are statistically different with respect to the corresponding covariate. *** Significant at the 1 percent level. **Significant at the 5 percent level. * Significant at the 10 percent level.

G, GG, GGG: first n children are girls.

Appendix B: Measures of birth intervals

We have four types of observations. Table 13 below gives further detail about the number of observations of each type:

1. Not censored, precisely measured; we observe:

 $t_n = (birth \ year \ of \ child \ (n+1) - birth \ year \ of \ child \ n) \times 12 + birth \ month \ of \ child \ (n+1) - birth \ month \ of \ child \ n$

So depending on the birth days of both children, we infer that $T_n \in [t_n - 1; t_n + 1]$.

2. Not censored, imprecisely measured; we observe:

$$t_n = (\text{age of child } n - \text{age of child } (n+1)) \times 12$$

So depending on the exact birth dates of both children, we infer that $T_n \in [t_n - 12; t_n + 12]^{41}$.

3. Censored, precisely measured; we observe:

 $t_n = (\text{year of survey - birth year of child } n) \times 12 + \text{month of survey - birth month of child } n$

We infer that $T_n > t_n - 1$.

4. Censored, imprecisely measured; we observe:

$$t_n = (age of child n) \times 12$$

We infer that $T_n > t_n$.

^{41.} E.g. if one child is 4 years old and the next one is 2 years old, we measure t = 24 and the two extreme cases are given by (i) the eldest will turn 5 the day following the survey while the youngest turned 2 the day before: the real t is 36; and (ii) the youngest will turn 3 the day following the survey while the eldest turned 4 the day before: the real t is 12.

Table 13: Number and frequence of observations by censoring and measurement status

Pooled	Precisely measured	Imprecisely measured	Total
Non-censored	621 (39%)	413~(26%)	1034 (65%)
Censored	441 (28%)	114~(7%)	555 (35%)
Total	1062 (66%)	527 (34%)	1589 (100%)

n=1	Precisely measured	Imprecisely measured	Total
Non-censored	314 (43%)	203 (28%)	517 (70%)
Censored	176 (24%)	44~(6%)	220 (30%)
Total	490 (66%)	247 (34%)	737 (100%)

n=2	Precisely measured	Imprecisely measured	Total
Non-censored	198 (37%)	132 (25%)	330 (63%)
Censored	156 (30%)	42 (8%)	198 (38%)
Total	354 (67%)	174 (33%)	528 (100%)

n=3	Precisely measured	Imprecisely measured	Total
Non-censored	109(34%)	78 (24%)	187 (57%)
Censored	109(34%)	28 (9%)	137 (43%)
Total	218 (67%)	106 (33%)	324 (100%)

A duration is considered as imprecisely measured when it is derived from the age of the child instead of the exact birthdate.

Appendix C: Fully parametric duration model

We start by defining a dummy R_n for long-term survivors at parity n, i.e. women who stop having children after the n^{th} birth. The probability of stopping is likely to depend on the characteristics of women after birth n summarized in the vector X_n ; we estimate the probability with a logit:

$$Pr(R_n = 1 \mid X_n) = p(X_n) = \frac{\exp(X_n'\alpha)}{1 + \exp(X_n'\alpha)}$$

For the women who have another child, the hazard function is now given by:

$$\lambda(t \mid X_n, \nu) = \lambda_0(t) \times \exp(X_n'\beta + \nu)$$

Where:

- $\nu \sim \mathcal{N}(0, \sigma)$: ν has a normal distribution such that $\mathbb{E}(\nu) = 0$ and $Var(\nu) = \sigma^2$.
- The baseline hazard function has a Weibull distribution with parameters λ and a.

$$\lambda_0(t) = \begin{cases} \lambda a(\lambda(t-8))^{a-1} & \text{if } t \ge 8\\ 0 & \text{if } t < 8 \end{cases}$$

This hazard function replicates two characteristics of the durations observed in our sample: (i) there is no exit before 8 months, and (ii) the inverted U-shape of the exit rate arises from the combination of an increasing baseline hazard together with unobserved heterogeneity.

The survival function conditional on R_n , X_n and ν allows us to retrieve the aggregate survival function conditional on X and ν .

$$S_1(t \mid R_n = 1, X_n, \nu) = 1$$

$$S_1(t \mid R_n = 0, X_n, \nu) = S(t \mid X_n, \nu) = \begin{cases} \exp(-(\lambda(t-8))^a \exp(X_n'\beta + \nu)) & \text{if } t \ge 8\\ 1 & \text{if } t < 8 \end{cases}$$

We derive the aggregate survival function conditional on X and ν :

$$S_1(t \mid X_n, \nu) = p(X_n) + (1 - p(X_n)) \times S(t \mid X_n, \nu)$$

Therefore, $S_1(t \mid X_n) \to p(X_n) > 0$ when $t \to \infty$. Using this specification, we are able to disentangle the effect of covariates, in particular Girls, Rivals and $Girls \times Rivals$, on the number of births and on the spacing of births. The vector α captures the impact on the probability to stop having children, whereas the vector β captures the impact on durations.

We estimate a multispell model in which the individual contribution to the likelihood $L_i(\theta \mid t_i, X_i, \nu_i)$ is given by :⁴²

- 1. $p(X_{1,i}) + (1 p(X_{1,i})) \times s(t_{1,i} \mid X_{1,i}, \nu_i)$ if woman i has exactly 1 child.
- 2. $\left((1 p(X_{1,i})) \times f(t_{1,i} \mid X_{1,i}, \nu_i) \right) \times \left(p(X_{2,i}) + (1 p(X_{2,i})) \times s(t_{2,i} \mid X_{2,i}, \nu_i) \right)$ if woman i has exactly 2 children.
- $3. \ \left((1 p(X_{1,i})) \times f(t_{1,i} \mid X_{1,i}, \nu_i) \right) \times \left((1 p(X_{2,i})) \times f(t_{2,i} \mid X_{2,i}, \nu_i) \right) \times \left(p(X_{3,i}) + (1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{1,i})) \times f(t_{1,i} \mid X_{1,i}, \nu_i) \right) \times \left((1 p(X_{2,i})) \times f(t_{2,i} \mid X_{2,i}, \nu_i) \right) \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{1,i})) \times f(t_{1,i} \mid X_{1,i}, \nu_i) \right) \times \left((1 p(X_{2,i})) \times f(t_{2,i} \mid X_{2,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 p(X_{3,i})) \times s(t_{3,i} \mid X_{3,i}, \nu_i) \right) \\ \times \left((1 -$
- $4. \ \left((1 p(X_{1,i})) \times f(t_{1,i} \mid X_{1,i}, \nu_i) \right) \times \left((1 p(X_{2,i})) \times f(t_{2,i} \mid X_{2,i}, \nu_i) \right) \times \left((1 p(X_{3,i})) \times f(t_{3,i} \mid X_{3,i}, \nu_i) \right)$ if woman i has 4 children and more.

Where $t_{n,i}$ is the duration (potentially right-censored) between births n and (n+1) for woman i; f(.) and s(.) are defined to explicitly allow for measurement approximations:

$$f(t_{n,i}) = (S(t_{n,i} - 1) - S(t_{n,i} + 1))^{P_{n,i}} \times (S(t_{n,i} - 12) - S(t_{n,i} + 12))^{(1 - P_{n,i})}$$

$$s(t_{n,i}) = S(t_{n,i} - 1)^{P_{n,i}} \times S(t_{n,i})^{(1-P_{n,i})}$$

Where $P_{n,i}$ is a dummy equal to 1 if the duration n is precisely measured for woman i. Hence, the contribution to the likelihood uses a confidence interval that depends on how precisely the duration is measured, instead of the density and survival functions.

Now, $\theta \equiv \{\alpha, \beta, \lambda, a, \sigma\}$ is the vector of parameters to be estimated. We start by considering the same parameters for all parities and compare the estimates to those found in the pooled Cox regression. Then we allow the parameters ⁴³ to vary depending on n, and compare the estimates to those found in the three separate Cox regressions. However, in the last specification, in order to keep enough degrees of freedom, we constrain the model and keep only the controls whose impact was significant in the estimation on all parities.

To compute the standard errors of e^{β_k} , we use the following approximation:

$$se(e^{\beta_k}) = e^{\hat{\beta_k}} \times se(\beta_k)$$

^{42.} The level of analysis is no longer the births as in the Cox model, but the women. Here, the number of observations is exactly equal to the number of clusters in the Cox model (=761).

^{43.} Except σ , the standard deviation of the unobserved heterogeneity. This is precisely the strength of the multispell model: random draws from the normal distribution are attributed once and for all to each individual, explaining simultaneously all durations.

Since there is no closed form expression for the expected likelihood, we use the technique of simulated maximum likelihood. We estimate $\mathbb{E}(L_i(\theta \mid t_i, X_i))$ with :

$$\widetilde{L}_i(\theta \mid t_i, X_i) = \frac{1}{H} \sum_{h=1}^{H} L_i(\theta \mid t_i, X_i, \nu_{i,h})$$

Where H = 60 is the number of random draws from a normal distribution for each individual.

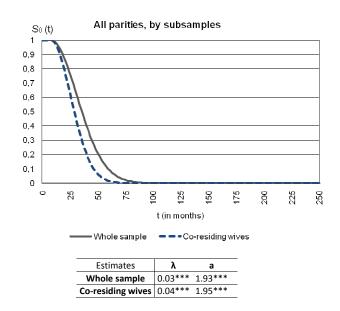
Last, we are able to compare across different categories of women, the probability of having another child, (1 - p(X)), and the expected duration conditional on X:

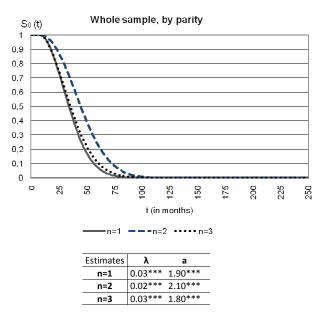
$$\mathbb{E}(T \mid X, \nu, \hat{\theta}) = \int_0^\infty S(u \mid X, \nu, \hat{\theta}) du$$

We also consider $(1-S(24 \mid X, \nu, \hat{\theta}))$. Again, we compute those quantities for the median individual (setting $\nu = 0$) and compare them to the ones obtained with the Cox estimation.

Appendix D : Additional estimates of the fully parametric model

FIGURE 4: Fully parametric estimation of baseline survival function





Significance levels: * p<0.10, ** p<0.05, *** p<0.01.

Appendix E: Robustness tests

Table 14: Robustness: Cox estimation (pooled, sample of co-residing wives)

Hazard ratios = e^{β_k}	Baseline specification	All parities	Ethnic groups
	(1)	(2)	(3)
Girls	1.07	1.12	1.08
	(.088)	(.089)	(.088)
Rivals	0.94	0.93	0.94
	(.112)	(.092)	(.114)
Girls imes Rivals	1.54**	1.49**	1.55**
	(.334)	(.308)	(.334)
Parities	$n \leq 3$	all n	$n \leq 3$
Controls	Yes	Yes	Yes
Ethnic group	No	No	Yes
Log-likelihood	-4607	-5633	-4604
Observations	1117	1271	1117
Clusters	515	518	515
Obs in cell : $Girls \times Rivals = 1$	64	68	64

Robust standard errors of e^{β_k} are in parentheses (clustered at the woman level). Significance levels (for $e^{\beta} \neq 1$): ***Significant at the 1 percent level. *Significant at the 5 percent level. * Significant at the 10 percent level.

Girls: first children are only girls; Rivals: there is at least one rival.

Sample: co-residing wives; column (1): baseline specification ($n \le 3$, no control for ethnic groups); column (2): we include all parities; column (3): we control for ethnic groups.

Controls include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, occupation, sector of activity of the husband, income of the husband, age difference with the husband and rank of preceding birth.

Table 15: Effect detectable after the first child: Cox estimation (Parity #1, by sub-samples)

Hazard ratios = e^{β_k}	Whole sample	Co-residing wives	Poorest half	Richest half
	(1)	(2)	(3)	(4)
\overline{G}	0.98	1.03	1.00	1.13
	(.095)	(.119)	(.167)	(.195)
Rivals	0.92	0.87	0.52**	1.17
	(.158)	(.180)	(.169)	(.332)
$G \times Rivals$	1.35	1.72*	2.95***	1.22
	(.323)	(.491)	(1.242)	(.503)
Baseline controls	Yes	Yes	Yes	Yes
Additional controls	No	Yes	Yes	Yes
Log-likelihood	-1889	-1295	-552	-624
Observations	737	500	252	248
Obs in cell : $Girls \times Rivals = 1$	57	38	22	16

Standard errors of e^{β_k} are in parentheses. Significance levels (for $e^{\beta} \neq 1$): ***Significant at the 1 percent level. *Significant at the 1 percent level.

G : first child is a girl; Rivals : there is at least one rival.

Column (2): sample restricted to wives living with their husband; this sample is then split on the median income into the poorest half in column (3) and the richest half in column (4).

Baseline controls mainly include characteristics of the woman: age at birth 1, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions.

Additional controls include: occupation of the wife, sector of activity of the husband, income of the husband, age difference with the husband.

Exact marginal-likelihood method to handle ties among non-censored durations.

Table 16: No preference for diversity: Cox estimation (pooled, sample of co-residing wives)

Hazard ratios= e^{β_k}	Co-residing wives
Boys	0.93
	(.082)
Rivals	1.11
	(.147)
$Boys \times Rivals$	0.90
	(.190)
Controls	Yes
Log-likelihood	-4610
Observations	1117

Robust standard errors of e^{β_k} are in parentheses (clustered at the woman level). Significance levels (for $e^{\beta} \neq 1$): *** Significant at the 1 percent level. *Significant at the 5 percent level. * Significant at the 10 percent level.

Controls include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, occupation, sector of activity of the husband, income of the husband, age difference with the husband and rank of preceding birth.

Breslow method to handle ties among non-censored durations (exact marginal-likelihood method is not available when standard errors are clustered).

TABLE 17: Common "intrinsic" son preference : Cox estimation (Parity #2, sample of women with at least one son)

Hazard ratios= e^{β_k}	Parity #2
BB	0.66***
	(.107)
Rivals	1.39
	(.295)
$BB \times Rivals$	1.08
	(.360)
Controls	Yes
Log-likelihood	-855
Observations	388

Standard errors of e^{β_k} are in parentheses. Significance levels (for $e^{\beta} \neq 1$): *** Significant at the 1 percent level. *Significant at the 1 percent level.

BB: first 2 children are boys; Rivals: there is at least one rival.

Controls include characteristics of the mother: age at birth 2, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions.

Exact marginal-likelihood method to handle ties among non-censored durations.

Table 18: Rivals = there is at least one male rival: Cox estimation (pooled)

Hazard ratios = e^{β_k}	Whole sample	Co-residing wives	Poorest half	Richest half
	(1)	(2)	(3)	(4)
Girls	1.00	1.09	1.13	1.05
	(.067)	(.087)	(.121)	(.133)
Rivals	0.86	0.81	0.69*	0.89
	(.112)	(.117)	(.148)	(.185)
Girls imes Rivals	1.37	1.58*	2.24**	1.19
	(.286)	(.404)	(.731)	(.436)
Baseline controls	Yes	Yes	Yes	Yes
Additional controls	No	Yes	Yes	Yes
Log-likelihood	-6569	-4606	-2112	-1956
Observations	1589	1117	569	548
Clusters	761	515	260	255
Obs in cell : $Girls \times Rivals = 1$	70	48	29	19

Robust standard errors of e^{β_k} are in parentheses (clustered at the woman level). Significance levels (for $e^{\beta} \neq 1$): ***Significant at the 1 percent level. *Significant at the 10 percent level. Girls: first children are only girls; Rivals: there is at least one male rival.

Column (2): sample restricted to wives living with their husband; this sample is then split on the median income into the poorest half in column (3) and the richest half in column (4).

Baseline controls mainly include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, rank of preceding birth.

Additional controls include : occupation of the wife, sector of activity of the husband, income of the husband, age difference with the husband.

Table 19: Rivals = there is at least one male rival : Cox estimation (separated by parity, whole sample)

Hazard ratios= e^{β_k}	Parity #1	Parity #2	Parity #3
\overline{G}	0.98		
	(.092)		
Rivals	0.83		
	(.191)		
$G \times Rivals$	1.58		
	(.473)		
GG		1.07	
		(.145)	
Rivals		1.06	
		(.214)	
GG imes Rivals		0.86	
		(.325)	
GGG			0.83
			(.201)
Rivals			0.61**
			(.147)
GGG imes Rivals			4.24**
			(2.448)
Controls	Yes	Yes	Yes
Log-likelihood	-1889	-1201	-640
Observations	737	528	324
Obs in cell: $Girls \times Rivals = 1$	42	21	7

Standard errors of e^{β_k} are in parentheses. Significance levels (for $e^{\beta} \neq 1$): *** Significant at the 1 percent level. *Significant at the 1 percent level.

Controls include characteristics of the mother : age at birth n, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions.

Exact marginal-likelihood method to handle ties among non-censored durations.

G, GG, GGG: first n children are girls; Rivals: there is at least one male rival.

Table 20: At least one rival, by gender: Cox estimation (pooled, sample of co-residing wives)

Hazard ratios = e^{β_k}	At least 1 male rival	At least 1 female rival	Both
	(1)	(2)	(3)
Girls	1.09	1.11	1.09
	(.087)	(.089)	(.088)
$Rivals_male$	0.81		0.79
	(.117)		(.124)
$Rivals_female$		0.97	1.07
		(.142)	(.161)
$Girls \times Rivals_male$	1.58*		1.47
	(.404)		(.484)
$Girls \times Rivals_female$		1.33	1.09
		(.343)	(.360)
Controls	Yes	Yes	Yes
Log-likelihood	-4607	-4609	-4607
Observations	1117	1117	1117
Clusters	515	515	515
Obs in cell : $Girls \times Rivals_male = 1$	48	na	48
Obs in cell : $Girls \times Rivals_female = 1$	na	40	40

Robust standard errors of e^{β_k} are in parentheses (clustered at the woman level). Significance levels (for $e^{\beta} \neq 1$): ***Significant at the 1 percent level. *Significant at the 5 percent level. * Significant at the 10 percent level.

Girls: first children are only girls; $Rivals_male$: there is at least one male rival; $Rivals_female$: there is at least one female rival.

Controls include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, occupation, sector of activity of the husband, income of the husband, age difference with the husband and rank of preceding birth.

Table 21: Rivals = number of rivals in inheritance shares : Cox estimation (pooled)

Hazard ratios = e^{β_k}	Whole sample	Co-residing wives	Poorest half	Richest half
	(1)	(2)	(3)	(4)
Girls	1.02	1.11	1.09	1.08
	(.067)	(.088)	(.119)	(.134)
Rivals	0.97	0.94	0.79**	1.03
	(.050)	(.056)	(.077)	(.043)
$Girls \times Rivals$	1.06	1.11	1.59***	0.97
	(.064)	(.087)	(.176)	(.056)
Baseline controls	Yes	Yes	Yes	Yes
Additional controls	No	Yes	Yes	Yes
Log-likelihood	-6570	-4608	-2109	-1956
Observations	1589	1117	569	548
Clusters	761	515	260	255
Obs in cell : $Girls \times Rivals > 0$	93	64	36	28

Robust standard errors of e^{β_k} are in parentheses (clustered at the woman level). Significance levels (for $e^{\beta} \neq 1$): ***Significant at the 1 percent level. *Significant at the 5 percent level. * Significant at the 10 percent level. Girls: first children are only girls; Rivals: number of rivals in inheritance shares.

Column (2): sample restricted to wives living with their husband; this sample is then split on the median income into the poorest half in column (3) and the richest half in column (4).

Baseline controls mainly include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, rank of preceding birth.

Additional controls include: occupation of the wife, sector of activity of the husband, income of the husband, age difference with the husband.

Table 22: Rivals = number of rivals in inheritance shares : Cox estimation (separated by parity, whole sample)

Hazard ratios= e^{β_k}	Parity #1	Parity #2	Parity #3
\overline{G}	1.00		
	(.093)		
Rivals	0.92		
	(.077)		
$G \times Rivals$	1.11		
	(.113)		
GG		1.06	
		(.141)	
Rivals		1.06	
		(.074)	
$GG \times Rivals$		0.95	
		(.103)	
GGG			0.85
			(.204)
Rivals			0.88
			(.088)
$GGG \times Rivals$			1.54**
			(.266)
Controls	Yes	Yes	Yes
Log-likelihood	-1890	-1200	-644
Observations	737	528	324
Obs in cell: $Girls \times Rivals > 0$	57	26	10

Standard errors of e^{β_k} are in parentheses. Significance levels (for $e^{\beta} \neq 1$): *** Significant at the 1 percent level. *Significant at the 1 percent level.

G, GG, GGG: first n children are girls; Rivals: number of rivals in inheritance shares.

Controls include characteristics of the mother: age at birth n, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, occupation, sector of activity of the husband, income of the husband, age difference with the husband and rank of preceding birth.

Exact marginal-likelihood method to handle ties among non-censored durations.

Table 23: Non-linear impact of the number of rivals: Cox estimation (pooled, sample of co-residing wives)

Hazard ratios = e^{β_k}	Nb rivals ≥ 1	Nb rivals ≥ 2	Nb rivals $= 1$	Nb rivals $= 1$,
				by gender
	(1)	(2)	(3)	(4)
Girls	1.11	1.10	1.05	1.06
	(.088)	(.091)	(.087)	(.089)
Nb_parts	0.94	0.96	0.87	
	(.056)	(.056)	(.152)	
Nb_male				0.75
				(.149)
Nb_female				1.30
				(.208)
$Girls \times Nb_shares$	1.11	1.09	1.90*	
	(.087)	(.082)	(.697)	
$Girls imes Nb_male$				2.20**
				(.866)
$Girls \times Nb_female$				0.99
				(.388)
Controls	Yes	Yes	Yes	Yes
Log-likelihood	-4608	-4039	-4097	-4095
Observations	1117	1005	1023	1023
Clusters	515	464	474	474
Obs in cell : $Girls \times Nb_parts > 0$	64	38	26	na
Obs in cell : $Girls \times Nb_male > 0$	na	na	na	21
Obs in cell : $Girls \times Nb_female > 0$	na	na	na	5

Robust standard errors of e^{β_k} are in parentheses (clustered at the woman level). Significance levels (for $e^{\beta} \neq 1$): ***Significant at the 1 percent level. *Significant at the 5 percent level. * Significant at the 10 percent level.

Girls: first children are only girls; Nb_shares : number of rivals in inheritance shares; Nb_male : number of male rivals; Nb_female : number of female rivals.

The sample of co-residing wives in column (1) is split on the number of rivals: column (2) includes only women with 2 and more rivals whereas columns (3) and (4) include only women with exactly 1 rival.

Controls include characteristics of the woman: age at preceding birth, place of residence, level of education, age at first marriage, being or not in her first marriage, living or not with the husband, having at least one dead child, having at least one child from previous unions, occupation, sector of activity of the husband, income of the husband, age difference with the husband and rank of preceding birth.